THE ASSESSMENT OF THE ABSOLUTE PLANIMETRIC ACCURACY OF AIRBORNE LASERSCANNING

J. Höhle

Aalborg University, Department of Planning, Fibigerstraede 11, DK 9220 Aalborg, Denmark, jh@land.aau.dk

Commission III, WG III/2

KEY WORDS: LIDAR, Point Cloud, DEM/DTM, Quality, Accuracy, Statistics, Specifications

ABSTRACT:

In acquisition and processing of Digital Elevation Models (DEMs) derived from airborne laser scanning (ALS) blunders and systematic errors occur. An assessment of the geometric quality of DEMs is necessary during production and before using the final DEM for an application. The vertical as well as the horizontal (planimetric) accuracy have to be assessed. Commonly agreed accuracy measures and procedures are necessary. The work of existing procedures and standards is analyzed. A new method to derive the absolute planimetric accuracy of ALS point clouds reliably and accurately is described. It is based on derivation of roof planes which are intersected to lines and points from the laser footprints. The coordinates of generated points are then compared with points determined by aerial photogrammetry. From the differences accuracy measures are derived. Tests regarding the type of error distribution are carried out in order to apply either standard accuracy measures or robust accuracy measures. The results of a practical test are used to assess the planimetric accuracy by means of various accuracy measures. Suggestions for a new standard for the assessment of the absolute planimetric accuracy of airborne lasercanning are made.

1. INTRODUCTION

The planimetric accuracy of airborne lasercanning influences the vertical accuracy in sloped terrain. It is important to know whether systematic shifts are present in the ALS data. These systematic shifts have to be small for many applications such as mapping and generation of 3D city models. Random errors may also be big. Detecting and eliminating blunders in the ALS data is an important task during the processing of ALS data. Some blunders may remain at the generation of Digital Terrain Models (bare earth data) because filtering and interpolation are a big source of errors. In order to have reliable values for the accuracy measures robust methods have to be applied when assessing the quality of DEMs derived by airborne lasercanning. The user of ALS data is mostly interested in their absolute accuracy. The efforts to determine the absolute planimetric accuracy are high if ground surveying is used. Photogrammetry is an alternative solution especially if photographs of the area exist or are taken simultaneously with the laser data. This contribution has the goal to present a methodology to derive the absolute planimetric accuracy of ALS data reliably and accurately. Commonly agreed standards on the accuracy of ALS are in demand and this investigation wants to contribute in defining the procedures and measures for quality control of airborne lasercanning.

2. ASSESSMENT OF THE ABSOLUTE PLANIMETRIC ACCURACY IN GENERAL

Absolute accuracies of ALS data are derived by comparison with reference data of superior accuracy. It is optimal to use well defined points, which are determined both by means of ALS and another method that can produce reference values with an accuracy which is at least 3 times higher. Such points which can be determined in both systems are named check points. Laser measurements are invisible on the ground and a measurement represents a small area called footprint. Well defined points do not exist in ALS. Planimetric errors result in elevation errors in areas with slope. A slope of 30° and a planimetric error of 1m will already result in a vertical error of 0.6m. The planimetric accuracy depends very much on the performance of the GNSS/IMU system. Medium priced IMU systems are quoted to have a nominal accuracy for the rotation angles of about 0.01°. If an IMU measures from 1000m above ground, the position of the footprint will be displaced by 0.2m. For economic reasons the flying altitude is often selected higher which then increases the displacement of the footprint. Other sources of errors are drift of the IMU as well as changes in the alignment between ALS and IMU-sensors. The assessment of the absolute planimetric accuracy is therefore an important part of the quality control. In order to assess the absolute planimetric errors of ALS several methods can be used.

Check points can be derived from laser footprints by intersecting planes (cf. Figure 1). Planes can be found on roofs of houses and their mathematical definition is possible by means of several laser footprints. There exist several types of roofs. Optimal are roofs of hip houses or cross gable houses, where three or four planes of different slope and exposition exist and which can be intersected to a point. These elevated points can be measured with superior accuracy by means of photogrammetry. The planimetric coordinates will serve as reference values. This approach is relatively inexpensive, especially when low-altitude
aerial images with orientation data exist. More details on the proposed method are presented in chapter 4 and in (Höhle&Pedersen, 2010).

Special targets can be placed on the ground before the flight. These targets are of special reflecting material, with differences in elevation and relatively large in size (Csanyi&Toth, 2007). The ALS data have to be very dense. The centre of the targets are measured by an independent method, e.g. by GNSS. This approach is time-consuming and requires good logistics.

The absolute accuracy of ALS data may also be determined by means of georeferenced scans of a terrestrial laserscanner. A study regarding this method has been published in (Fowler&Kadatskyi, 2011).

Several authors deal with the relative accuracy of ALS data in order to connect strips. In (Vosselman, 2008) ridge lines are derived from the ALS data of adjacent strips. The distance between the middle of the ridge line of the first strip and the ridge line of the second strip are used as observations. The offsets between the strips are then calculated by least squares adjustment. The remaining residuals are used as measures of the relative planimetric accuracy. Other authors use the distance between points of one strip and a triangulated mesh (TIN) of a second strip (Maas, 2002). This method assumes that the triangles represent the actual surface, which may not always be the case.

In (van der Sande et al., 2010) planar surfaces of roofs and dykes are used and parameters of the planes are derived by the RANSAC method. The points of the corresponding plane of the second strip are used to determine the distance to the derived plane of the first strip. These distances are then minimized by least squares adjustment where six parameters of a 3D affine transformation are determined. The mean and the standard deviation of the residuals after the strip adjustment are used as measures for the relative accuracy.

In (Kager, 2004) a combination of three roof patches is used to adjust the strips absolutely. The roofs have to have a different exposition, a high inclination, and they should be situated nearby. The parameters of the three planes are determined by means of four or more points on the roof measured by ground surveying. Three planes are intersected to virtual points and their coordinates are compared with the coordinates derived from the ALS data using intersection of three planes. The residuals at such virtual control points are a measure of the absolute accuracy. Such an assessment with points used in the adjustment is, however, not independent. Independent checkpoints can also be generated from the roof triples. The absolute accuracy of ALS can then be derived correctly. The ground surveying of many roof planes may become expensive.

Another approach to check the planimetric accuracy of ALS data is the use of the intensity image, which is generated together with the spatial data. Paint stripes on asphalt, for example, may be visible in the intensity image. Their position can be compared with the position derived by ground measurement. A high density of the footprints and/or a large width of the stripes are required in order to detect such stripes. The distance between footprints should be half of the width of the stripes. The error in the determination may reach half of the spacing between the footprints. Therefore, this method is not very usable for an accurate assessment of the planimetric accuracy of ALS data.

3. ACCURACY MEASURES

Accuracy measures are derived from the differences between the ALS value and the reference value. The sign of the difference is important and should always be defined as an ‘error’ (ALS-value – reference). From these original differences standard accuracy measures are calculated, these are the Root Mean Square Error (RMSE), the Mean Error (µ) and the Standard Deviation (σ).

The Mean Error indicates that the ALS data are shifted with respect to the reference. Gross errors may exist in the ALS data but they should not influence the accuracy measures. They can be eliminated by means of a threshold if only very few gross errors exist. A histogram of the errors will inform whether the distribution of the errors is normal. The curve for a normal distribution (Gaussian bell curve) can be superimposed. If the curve does not match the data very well, the distribution is not normal.

A better diagnostic plot in order to detect a deviation from the normal distribution is the so-called quantile-quantile (Q-Q) plot. The quantiles of the empirical distribution function are plotted against the theoretical quantiles of the normal distribution. If the actual distribution is normal, the Q-Q plot yields a straight line. Big deviations from the straight line indicate that the distribution of the errors is not normal.

If the histogram of the errors or the Q-Q plot reveals non-normality, robust accuracy measures should be applied. They are based on the Median of the distribution. The Median is the middle value if all errors are put in an order, starting from the lowest value to the highest value. The Median is named the 50% quantile and denoted as Q(0.5). It is a robust estimator for a systematic shift of the ALS data. Another robust accuracy measure is the Normalized Median Absolute Deviation (NMAD). It corresponds to the standard deviation when no outliers exist.

A robust and distribution free description of the measurement accuracy is obtained by reporting quantiles of the distribution of the absolute errors. For example, the 95% quantile means that 95% of the errors have a magnitude within the interval [0, Q(0.95)]. The remaining 5% of the errors can be of any value making the measure robust against up to 5% blunders. Another important measure is the 68.3% quantile of the absolute errors. It indicates the value where all differences smaller than this value amount to 68.3% of all errors. This percentage is also used to define the standard deviation (1-σ) at normal error distribution. The meaning of the robust accuracy measures can be explained by means of Figure 2 where the quantiles (Q) are plotted as function of the probability (p). Normal distribution of the errors is assumed and the unit of quantiles is the standard deviation.

If absolute values of the errors are used, Q(0.683) corresponds to 1-σ and Q(0.95) to 1.96-σ. The 50% quantile of the absolute values of the errors (red curve) equals to 0.67-σ and is named Median Absolute Deviation (MAD). Multiplication of MAD by the factor 1.4826 is then the Normalized Median Absolute Deviation (NMAD). At normal distribution the NMAD value corresponds to the standard deviation (1-σ). All of the robust

\* The differences between the measured coordinates and the reference coordinates can also be modelled, e.g. by means of a 2D affine transformation. The use of the original differences is recommended.
accuracy measures are summarized in Table 1. In the assessment of the horizontal accuracy, the assessment has first to be done for the single coordinate errors (ΔE, ΔN).

Figure 2. Robust accuracy measures: Median, Q(0.68), and Q(0.95). The quantile function Q(p) for absolute errors (red line) shows that Q(0.68) corresponds to 1·σ in case of normal distribution. When original errors are used (stippled black line) the difference dp=0.68 corresponds to the range of ±1·σ.

Table 1. Robust accuracy measures for a variable x

<table>
<thead>
<tr>
<th>Quantile</th>
<th>Q(x)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Median (50% quantile)</td>
<td>$\hat{Q}_{x}(0.5) = m_x$</td>
</tr>
<tr>
<td>Normalized Median Absolute Deviation</td>
<td>NMAD=1.4826- median(</td>
</tr>
<tr>
<td>68.3% quantile</td>
<td>$\hat{Q}_{x}(0.683)$</td>
</tr>
<tr>
<td>95% quantile</td>
<td>$\hat{Q}_{x}(0.95)$</td>
</tr>
</tbody>
</table>

Also radial errors can be generated by

$$r_i = \sqrt{(\Delta E_i - \mu_E)^2 + (\Delta N_i - \mu_N)^2}$$  \hspace{1cm} (1)

and then treated as absolute errors.

The confidence intervals (CI) of the accuracy measures have also to be calculated using a confidence level of 95%. For the robust accuracy measures the bootstrap method can be applied (Höhle&Höhle, 2009). The assessment of the horizontal accuracy has to be carried out by means of a sufficient number of checkpoints. They should be randomly distributed over the whole DTM area.

The planimetric errors can be visualized graphically together with an ellipse of constant probability, e.g. p=0.95. The parameters of the ellipse (semi axes and angle between major axis and Easting) are derived by means of formulae published in (Mikhail 1976). The centre of the ellipse has the coordinates $\mu_E$ and $\mu_N$. The reduced radius ($r'$) is then:

$$r' = \sqrt{(\Delta E_i - \mu_E)^2 + (\Delta N_i - \mu_N)^2}$$  \hspace{1cm} (2)

Its distribution is derived from the joint (bivariate) distribution. There is a wish to characterize the planimetric error by a single value, for example by $\sigma_r$ or $\sigma_c$. Other suggestions derive measures starting from the standard deviations of the two coordinate errors and the probability of a standard ellipse:

**Mean Square Positional Error (MSPE)**

$$\sigma_P = \sqrt{\sigma_E^2 + \sigma_N^2}$$  \hspace{1cm} (3)

The MSPE is also named ‘point error’ and symbolized by $\sigma_P$. The probability that radial errors ($r_i$) occur less than $\sigma_P$ depends on the ratio $\sigma_N/\sigma_E$. If $\sigma_E=\sigma_N$ the probability that $r_i<\sigma_P$ is $p=0.632$.

**Circular Standard Error ($\sigma_c$)**

This error is defined by $1.0\cdot\sigma_c$, and $p[r_i<\sigma_c]=0.393$. An approximation is obtained by

$$\sigma_c \approx 0.5(\sigma_E+\sigma_N)$$  \hspace{1cm} (4)

**Circular Error Probable (CEP)**

The definition of CEP is $p[r_i<\text{CEP}]=0.5$.

$$\text{CEP}_{0.50} \approx 1.177 \cdot \sigma_c = 0.589(\sigma_E+\sigma_N)$$  \hspace{1cm} (5)

The calculation after formulae (4) and (5) are approximations and only valid when the relation $\sigma_{\text{min}}/\sigma_{\text{max}}$ is not smaller than 0.6 (Congalton&Green, 2009). The CEP may be used with other probabilities, e.g. with $p=0.95$. Then the calculation is $\text{CEP}_{0.95} \approx 2.447\cdot\sigma_c$. The factor $k=2.447$ is derived from the $\chi^2$ - distribution with two degrees of freedom (cf. Figure 3).

In (Borre, 1990) the planimetric error is defined by:

$$\sigma_P = \sqrt{\frac{\sigma_E^2 + \sigma_N^2}{2}}$$  \hspace{1cm} (6)

In Figure 3 the mentioned accuracy measures may be compared with regard to their probability in the case $\sigma_E=\sigma_N$. Many different accuracy measures are not very useful and a selection has to be made. All mentioned accuracy measures will be used in the practical tests with the method of derived check points. A recommendation will be made which of the accuracy measures should be used in specifications and standards.
In (ASPRS, 2005) and (Congalton & Green, 2009) the American standards for horizontal accuracy measures are described. These standards derive the standard deviation from the differences between the errors and the RMSE estimate (and not the Mean). A circular as well as an elliptical statistic is applied using RMSE values for the radius or coordinates respectively. A confidence interval on the estimate of RMSE is calculated at 95% probability. The NSSDA circular statistic, for example, corresponds to 1.731*RMSE.

4. A PROCEDURE FOR THE ASSESSMENT OF THE PLANIMETRIC ACCURACY

The use of houses is the base of the method proposed in (Höhle&Pedersen). Suitable houses are hip houses and cross gable houses (cf. Figure 1). The parameters of the planes are derived from laser footprints using robust adjustment. This means that observations of objects above or below the plane (e.g. chimneys, windows) are down-weighted and therefore have no influence on the results. Several iterations are carried out in order to find accurate solutions for the parameters of planes. Three adjacent planes are intersected to a point. For the intersected points the precision and confidence ellipses are derived and analyzed. Large and deformed ellipses will indicate a poor determination of the points. The derived spatial coordinates of these check points are compared with reference values derived by photogrammetry. A few ground control points are required in order to determine the exterior orientation data of the images. These six parameters may also be known from a preceding aerotriangulation. The well-defined checkpoints on top of the houses are manually measured. The achievable accuracy of this photogrammetric point determination when using modern digital cameras from an altitude of 1000m is a few centimetres. The images are also used to measure the corners of the roofs in order to extract all footprint inside a roof areal. The extraction of check points is used to measure the corners of the roofs in order to extract all rooftop points and the absolute accuracy of coordinates and intersected points. It is assumed that the upper roof points have the same accuracy. Having such a high accuracy these measurements are qualified as reference data.

5. PRACTICAL TESTS

The practical tests for the determination of the planimetric accuracy of ALS data have been carried out with the original point cloud of the new Danish DEM. The data are collected by a Lite Mapper 5600 scanner produced by Riegel/IGI mbH. The average density of the point cloud was 0.45 points/m² only. The overlap between strips was at least 5% of the swath width. The Inertial Measurement Unit (IMU) determined the attitude of the laser scanner with a nominal accuracy of 0.004° for roll and pitch angles. The footprint of the laser beam had a diameter of 0.5m. In the assessment of the horizontal accuracy some conditions have to be fulfilled. The roof have to be plane with certain slope and containing more than four footprints. This condition has been checked by the programs. Additional data like orthoimages and maps helped in the selection of suitable roofs (cf. Figure 4). The reference data and other roof points were derived from images taken by the large format digital frame camera DMC of Hexagon/Intergraph. The images had an overlap of 60% and a ground sampling distance of GSD=10cm.

The photogrammetric determination of reference data used four images.

Figure 4. Orthoimage and vector map are used to select suitable roofs. Note that not all of the roofs contain footprints (red areas)

The measuring of the image coordinates occurred on the screen of a desktop computer. The same point had to be measured in two or more images. The exterior orientation of the aerial images was determined by bundle adjustment. Only four Ground Control Points (GCPs) were used. The processing was carried out by open-source software (IFP, 2009) running in a personal computer. The GCPs as well as a few checkpoints (for the determination of the quality of the orientation data) have been measured by means of GPS/RTK. The reference system was UTM with the coordinates Easting (E) and Northing (N). The orientation of the images proved to be very accurate. The standard deviation of the unit weight was 4.0μm in the image. The quality of the orientation was assessed by independent checkpoints. A RMSE of 4.2cm has been found for each of the two planimetric co-ordinates. It is assumed that the upper roof points have the same accuracy. Having such a high accuracy these measurements are qualified as reference data.

6. RESULTS

The analysis of the results will include the precision of the intersected points and the absolute accuracy of coordinates and radial errors. The precision of the intersected points is calculated for each point. An average of all standard deviations is σ_E=16cm and σ_N=13cm. The precision of the derived points differs, but the majority of the points have a relatively high precision. The comparison with the spatial coordinates of 53 reference points reveals absolute coordinate errors of σ_E=26 cm in Easting and σ_N=18cm in Northing (cf. Table 3). There are systematic errors of μ_E=+8cm and μ_N=+16cm, which made the RMSE values somewhat higher than the standard deviation (RMSE_E=27cm, RMSE_N=24cm). In the plot of all errors together with the 95% confidence ellipse (cf. Figure 5) it can be seen that the centre of the ellipse is displaced and three points are outside the ellipse. The 95% confidence ellipse has semiaxes of a=0.64m and b=0.44m. The probability is based on bivariate normal distribution where both coordinate errors are considered to be independent and occur jointly. Applying a threshold of 3*RMSE revealed that there was one blunder in each of the coordinates. Therefore, robust accuracy measures had to be applied. The robust accuracy measures for the two
single coordinates and their 95% confidence intervals are contained in the lower part of Table 3. The Median is smaller than the Mean, the NMAD is smaller than the Standard Deviation and the Q_{0.683}(0.683) is smaller than the RMSE. It means that the blunders have falsified the standard accuracy measures and their values are not correct.

changing with the relation \( \sigma_{\text{meas}} / \sigma_{\text{true}} \) and is given for the special case \( \sigma_{\text{meas}} = \sigma_{N} \) (cf. Table 5).

<table>
<thead>
<tr>
<th>Probability</th>
<th>CEP [m]</th>
<th>( \sigma_{r} ) [m]</th>
<th>( \sigma'_{r} ) [m]</th>
</tr>
</thead>
<tbody>
<tr>
<td>p=0.393</td>
<td>0.22</td>
<td>0.23</td>
<td>0.22</td>
</tr>
<tr>
<td>p=0.500</td>
<td>0.26</td>
<td>0.27</td>
<td>0.26</td>
</tr>
<tr>
<td>p=0.632</td>
<td>0.31</td>
<td>0.32</td>
<td>0.31</td>
</tr>
<tr>
<td>p=0.683</td>
<td>0.33</td>
<td>0.34</td>
<td>0.33</td>
</tr>
<tr>
<td>p=0.950</td>
<td>0.54</td>
<td>0.55</td>
<td>0.54</td>
</tr>
</tbody>
</table>

Table 5. Planimetric accuracy by one value (probability for the case of \( \sigma_{\text{meas}} = \sigma_{N} \)). The underlined values are the radii of the standard circle (\( k=1.0 \))

The CEP- and \( \sigma'_{r} \)-values (cf. Table 5) are in good agreement with the quantiles of the unbiased radius (\( Q_{r} \)) (cf. Table 4). The Mean Square Positional Error (MSPE=\( \sigma_{r} \)) is calculated by equation (3) with \( \sigma \) =32cm. Its exact probability is \( p=0.570 \) at the ratio \( \sigma_{N} / \sigma_{N} = 0.69 \). If this ratio is different, the probability will change, e.g. at \( \sigma_{N} / \sigma_{N} =1.0 \) to \( p=0.632 \). The better solution is, therefore, to derive quantiles with constant probability from the radial errors (\( r' \)). The 95% quantile was determined with \( Q_{r(0.95)}=0.56 \)m. In Figure 6 the accuracy measures based on the same probability (95%) are depicted and can, therefore, be compared.

The error derived from the semi-axes of the confidence ellipse and the circular error probable (CEP 0.95) are smallest. The accuracy measures based on the radius (\( r \)) have higher values than the ones based on the unbiased radius (\( r' \)). \( Q_{r} \) is nearly of the same size as the CEP 0.95.

7. DISCUSSION

The following discussion will comprise the two topics, the used method in the accuracy assessment and the applied accuracy measures. The used method applied photogrammetry to derive accurate and reliable reference data. In this investigation the accuracy of the planimetric coordinates was RMSE=4.2cm. The imagery was taken with GSD=10cm and is normally used for mapping and orthoimage production. The ideal proposition is that the imagery is taken together with ALS data acquisition and from relatively low altitudes. A large number of checkpoints can be generated economically in this way. The derivation of the coordinates of checkpoints from ALS data was carried out by modelling of planes and intersecting them to points. Roofs of hip- and cross gable houses are suitable. The
combination of three gable houses is also possible. The planarity of the roofs does not always exist. Objects above or below the plane have to be eliminated from the point cloud. The used robust adjustment eliminated such laser footprints. The sufficient number of footprints and inclination of the roofs will produce accurate check points. The plotting of confidence ellipses will disclose weak intersections. The assessment of the planimetric accuracy in principle be combined with the assessment of the vertical accuracy. The accuracy of elevations derived by means of photogrammetry was not accurate enough in this test. Elevations of checkpoints on flat ground can accurately and easily be determined by means of geodetic measurements, e.g. by GNSS. The measurement of inclined roofs by means of GNSS is not very feasible. Imagery may not be available as in this case. However, the simultaneous acquisition of ALS and imagery will be more used in future than today. Most of the DEM applications require complete, reliable and interpreted elevations together with other data, below the plane have to be eliminated from the point cloud. The planimetric accuracy may in principle be combined with the assessment of the vertical accuracy. The assessment of planimetric accuracy of ALS data derived by airborne laser scanning requires the unknown reviewers are thanked for their constructive criticism of this article.

REFERENCES


ACKNOWLEDGEMENTS

The National Survey and Cadastre of Denmark is thanked for providing ALS data. C. O. Pedersen supported the author in programming the method of assessment the planimetric accuracy of ALS data. The unknown reviewers are thanked for their constructive criticism of this article.

8. SUGGESTION OF A NEW STANDARD FOR PLANIMETRIC ACCURACY OF ALS

The assessment of the planimetric accuracy of ALS data can be carried out using sloped roofs of houses. Well-defined checkpoints are derived from a large number of footprints covering three roof planes and intersecting the modelled planes to points. Accurate coordinates of these check points can be determined by means of photogrammetry. The errors in the coordinates have to be analyzed with respect to blunders and distribution. If the distribution of the errors is normal, the standard accuracy measures (Mean, Standard Deviation, and RMSE) are applied for the coordinates and for the radii. In the case of non-normal distribution the robust accuracy measures have to be used. These are the Median, the NMAD for both coordinates and the 95% quantile of the unbiased radial error (Q(0.95)). All accuracy measures have to be supplemented by confidence intervals which will disclose whether the number of checkpoints were sufficiently high. A plot of all single errors together with a 95% confidence ellipse will display the overall geometric quality of the DEM.