

OPTIMAL INFORMATION EXTRACTION OF LASER SCANNING DATASET BY SCALE-ADAPTIVE REDUCTION

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ABSTRACT:

3D laser technology is widely used to collocate the surface information of object. For various applications, we need to extract a good perceptual quality point cloud from the scanned points. To solve the problem, most of existing methods extract important points based on a fixed scale. However, geometric features of 3D object come from various geometric scales. We propose a multi-scale construction method based on radial basis function. For each scale, important points are extracted from the point cloud based on their importance. We apply a perception metric Just-Noticeable-Difference to measure degradation of each geometric scale. Finally, scale-adaptive optimal information extraction is realized. Experiments are undertaken to evaluate the effective of the proposed method, suggesting a reliable solution for optimal information extraction of object.

1. INTRODUCITON

LiDAR technology is highly valuable in many application domains such as urban planning, geography, cultural heritage protection and others because of its accuracy, speed and penetrability. However, the high density of LiDAR data leads to an enormous increase in data volume, which brings great challenges with respect to data storage, processing, display and transmission (Liu and Zhang, 2011). Therefore, it is necessary to extract the optimal information from the original points. In principle, important points should be kept and points that are not important should be reduced. However, as a result of the increasing availability of high density data, some relatively important points are also eliminated to achieve a higher reduction ratio, and some points that are not important should also be kept to preserve the geometric information of surface.

Various approaches have been proposed to tackle this issue. These algorithms can be classified into three categories: the random method, the point subtractive method and the point additive method (Chen, *et.al.*, 2015). Immelman *et.al.* (2011) and Anderson *et.al.* (2005) applied the random extraction method. To meet the reduction ratio, a portion of points are randomly reduced. This method is simple and fast, but it does not consider the point importance so it has low accuracy. Oryspayev *et.al.* (2012) applied the point subtractive method, which reduces points with lower errors until a tolerance is reached. The error at each point is the distance from the point to its corresponding triangle constructed by the new local points after removing this point. This method is time consuming that it is impractical to reduce huge dataset. Different from that, Moening *et.al.* (2003) proposed a point additive reduction method. Firstly, randomly take a subset from the input point cloud to establish the 3D Delaunay triangular mesh. Then define a precise distance function on this subset. Finally according to the distance from point to its corresponding

triangle, add points to this subset until the error threshold or the desired number of points is reached.

To our knowledge, viewing an object (*e.g.*, tree), we can notice geometric features of different spatial scale. For small spatial scale feature, leaf features can be noticed. And for large one, branch and tree trunk features can also be found. Geometric features of multi spatial scales form the complete information of the object. However, the above methods are performed at a unique spatial scale, which is doomed to be incomplete and misleading.

In order to derive and analyse comprehensive information of one object, multi-scale scheme is often account for this phenomenon. Arefi *et.al.* (2008) proposed an automatic multi-scale modeling approach in three scales of detail. This method constructs the buildings which are formed by combination of flat roof, gabled roof and hipped roof segments. The examples illustrate this multi-scale representation of city buildings performs quite well. For free-form object, characteristics of curve surface are also considered in methods to retain the feature information of each scale. Pauly *et.al.* (2006) applied the surface diffusion equation to the discrete multi-scale surface representation. The benefit of this hierarchy is the decoupling of shape and detail at different scales. Luo *et.al.* (2011) proposed a multi-scale representation approach based on random walks to generate archaeological line drawings automatically instead of manual drawings. This method reduces redundant lines detected on the rough and noise surface. Additionally, some constructions of three dimensional scale space (Mokhtarian *et.al.*, 2001; Schlattmann *et.al.*, 2006) replace two dimensional pixel densities with three dimensional coordinates directly. These approaches produce erroneous results since the extrinsic geometry of the original data was modified. To solve the above problems, Bariya *et.al.* (2012) put forward a registration and recognition method based on scale-dependent features. In this method, normal vector map was used instead of the original

range image. The Intrinsic Geometric Scale of feature points was used to construct scale-dependent features. However, the target of this method is range image. For a three dimensional object, many projection angles should be considered. Similarly, Novatnack *et al.*, (2007) and Hua *et al.*, (2008) unwrapped the surface of model onto a two dimensional image. The scale space was constructed based on the geometric attributes retained on the image. However, when a surface patch containing complex features is squeezed into a very small domain, problems will appear.

In this paper, we propose a multi-scale extraction method to describe geometric features of different spatial scales. The small scale points describe the small features while large scale points focus on the features of larger spatial scale and ignore the small ones. If the geometric scale selected is smaller, data redundancies may exist; if the geometric scale selected is larger, many meaningful information may be lost. To extract optimal information of point cloud, we measure the visual degradation of point cloud of each scale. Unnecessary and unnoticeable geometric features are reduced as much as possible to provide a good quality data for further applications.

The rest of the paper is structured as follows: Section 2 and Section 3 describes our proposed method to construct the geometric multi-scales based on radial basis function model, and select optimal scale based on a perceptual metric. We report the outcomes of a number of experiments undertaken to demonstrate the validities of the proposed method in Section 4. Finally, in Section 5 we draw our conclusions.

2. SURFACE VARIATION AND IMPORTANCE MEASUREMENT

2.1 Surface Variation

Apply PCA and local covariance statistics to estimate the normal vector of each point based on its neighbourhood points (Nurunnabi *et al.*, 2015). The calculated normal vectors of two adjacent points may have opposite directions. To ensure the accuracy of surface variation, consistent propagation of normal vectors is realized by traversing minimum cost spanning tree (König *et al.*, 2009). For a local area, calculate the cosine value between normal vectors of current point and one neighbour by:

$$C_i = 1 - \vec{n}_0 \cdot \vec{n}_i \quad (1)$$

The upper value is between 0 and 2. The surface variation of current point is evaluated by the mean error of neighbourhood cosine values, as:

$$S_0 = \frac{\sum_{i=1}^n |C_i - \text{mean}|}{n} \quad (2)$$

Here n is the number of neighbours, mean is the mean value of neighbourhood C values. This value describes the surface variation since the value is larger when local surface has larger variation.

2.2 Importance Measurement

The key to construct multi-scales is to determine whether one point is important at a given scale. In this section, we propose an effective important metric based on radial basis function. This function considers the influence of neighbourhood point distribution on the current point, it is a successful tool for the approximation. The function is assumed to have the form:

$$s(p) = \sum_{j=1}^N \lambda_j \varphi(\|p - p_j\|) + c(p), c \in S^d \quad (3)$$

Where $\|\cdot\|$ is the Euclidean norm on \mathbb{R}^d , $c(p)$ is the polynomial part and S^d denotes the linear space containing polynomials in d variables. Many classical choices for radial basis functions have been proposed (e.g. Gaussian, multi-quadric and cubic). To reduce the calculation complexity of RBF, Wendland (1995) put forward unified formula of basic function, defined as:

$$\varphi(r) = \begin{cases} (1-r)^q p(r), & 0 \leq r \leq 1, \\ 0, & 1 < r, \end{cases} \quad (4)$$

Various forms of $\varphi(r)$ with continuity of C^0, C^2, C^4 was given.

Here C^2 continuity: $\varphi(r) = (1-r)_+^4 (4r+1)$ is applied popularly. If the distance from one neighbour to current point is smaller than support radius r , then $\varphi(r) = 0$. This local supporting property reduce the calculation complexity.

We evaluate the importance of one point by two aspects: surface variation and the distribution of neighbourhood points. The *Importance* metric is defined as:

$$\begin{cases} I_0 = S_0 \exp(-w \sum_{i=1}^N m_i \varphi(\|P_i - P_0\|/\lambda)) \\ m_i = \frac{S_i}{\sum_{j=1}^N S_j} \end{cases} \quad (5)$$

Here S_0 is the surface variation of current point P_0 , λ is the support radius factor, P_i is one point from the valid supporting region, w is the weight coefficient, deciding the degree of influence of neighbours on current point, m_i is the proportion of neighbourhood surface variation. In the formula (5), RBF is used to measure the contribution of neighbourhood point to current point. This contribution depends on the number and spatial distribution of neighbour points. When the neighbour points distribute densely, the contribution is large, *importance* will decrease, vice versa. This characteristic of the formula suggest that the influence of neighbourhood distribution can be described well.

3. MULTI-SCALE CONSTRUCTION AND OPTIMAL SELECTION

3.1 Edge Points Detection

Surface variation outlier values will appear in the edge areas, we apply an angle criterion method to detect the edge points. The spatial distribution characteristics of local points is used to detect the edge points. If the neighbours of one point distribute on one side, this point is regarded as edge point; if the neighbours distribute around this point uniformly, it is regarded as internal point, as shown in Figure 1.

The specific procedures are: Firstly, local tangent planes are constructed by one point and its neighbours, and project neighbours to this plane to get a 2D point set; Then calculate angles formed by two consecutive projected neighbours to the current point, and sort all the angles in decreased order; Finally, get the largest gap to judge whether it is edge point.

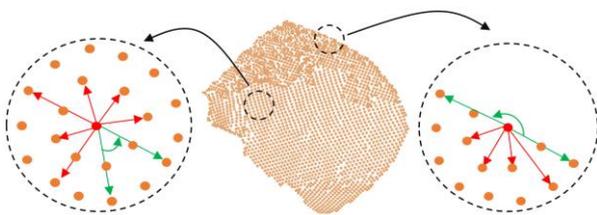


Figure 1. Neighbourhood distribution of one inner point and one edge point

3.2 Extraction of multi-scale Points

Based on importance metric and the detected edge points, we apply the following procedures to extract points of one scale:

- Suppose the Final Point Set of current scale is empty. Surface variation of each point is calculated based on the neighbourhood size of current scale.
- Sort original points by their surface variation values in decreasing order, and select the variation value of the point at 90% as the *Importance* threshold.
- Take one point (non-edge point) from the sorted point set successively to the Final Point Set. Calculate the *Importance* of this point based on the new neighbours in Final Point Set by Formula 5. If *I value* is larger than threshold, keep it, or remove it from Final Point Set.
- Repeat step c until all the points of original point set is considered. Take the Final Point Set together with the smaller scales as current scale points.

3.3 Optimal Scale Selection

For a surface, removing a point will generate a stimulus to human vision. To measure the perceptual impact, Just-Noticeable-Difference (JND) is used (Xu *et al.*, 2014). However, the application of JND is limited since it needs complex skeleton extraction. In this section, we improve JND measurement by replacing the skeleton with 3D smoothed surface.

When a point is removed, its local geometric information is represented by its closest remaining point. We use $\Delta\rho$ to describe the change when point A is removed from the mesh (as show in Figure 2), point B is the nearest remaining point of A. ρ is defined as the perception distance from the closest

remaining point to the smoothed surface. The stimulus variation is defined as:

$$K = \frac{\Delta\rho_{AB}}{\rho} = \frac{|r_A - r_B|}{r_B} \quad (6)$$

Here r_A and r_B are the distances from point A and B to the smoothed surface. K is the JND threshold. According to the Formula, removing point A has less stimulus than removing point C. Due to Webber's equation, the stimulus value less than K is not perceptible to human vision. The degradation will be recorded if the stimulus is larger than K. In this paper, experiments suggest $K = 0.8$.

To generate the 3D smoothed surface, we extend the 2D Gaussian kernel. The 3D Gaussian kernel is defined as:

$$G(i, j; \delta) = \frac{1}{2\pi\delta^2} \exp\left[-\frac{1}{2\delta^2} d_{ij}^2\right] \quad (7)$$

Here δ is the mean square root of Gaussian kernel function, d_{ij} is the distance from neighbourhood point j to current point i . This process is repeated for each point, and the new points define the smoothed surface. Similar to 2D smoothing, the larger mean square root is, the larger geometric features will be smoothed out. Larger mean square root is selected in this paper.

Based on JND model, we apply salient information distortion metric (Shi *et al.*, 2010) to measure the degradation of each scale. According to the degradation value, we select the optimal scale with least points to reserve the most perceptual information.

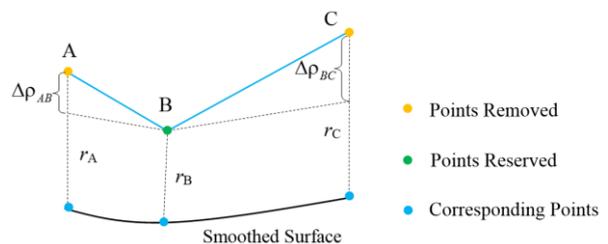


Figure 2. Stimulus variations generated by removing points

4. EXPERIMENTAL RESULTS AND ANALYSIS

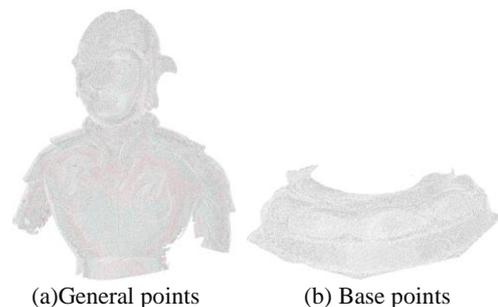


Figure 3. Experimental point clouds.

To evaluate the efficiency of proposed method, General and Base are selected for experiment. They are scanned by Handyscan 3D scanner with the average span of point clouds about 1.0mm and 0.2mm, respectively. Both of them have multi-scale of geometric details and rich redundancies.

4.1 Detection of Edge Points

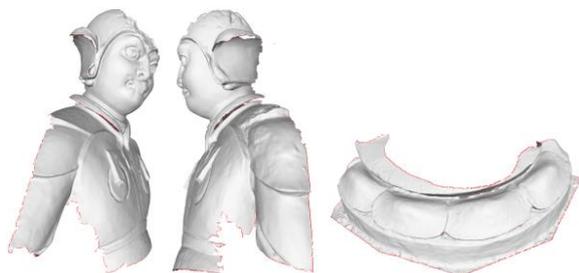
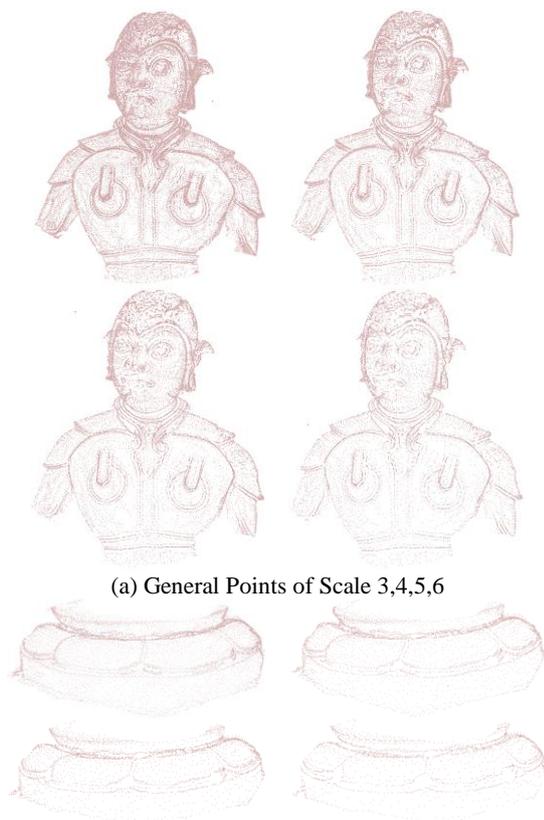


Figure 4. Edge points detected

Some outlier edge points may be introduced by surface variation. They will affect the construction of multi-scale. From Figure 4 we can see that the edge points of two point clouds can be detected effectively (red dots indicate the detected edge points). This insures the validity of extraction of multi-scale points.

4.2 Extraction of Multi-scale Points

Extracted points of scale 3,4,5,6 are shown in Figure 5. It suggests that important points of different scales can be well reserved with a suitable point span; And in smooth areas, local maximum feature points can also be reserved so that no obvious holes can be found. In addition, points of different scales reflecting different scale features can well represent the geometric information of object.



(a) General Points of Scale 3,4,5,6
 (b) Base points of Scale 3,4,5,6
 Figure 5. Multi-scale of points extracted

4.3 Optimal Scale Selection

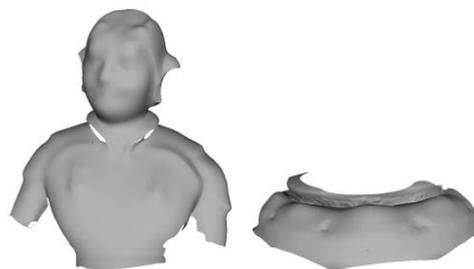


Figure 6. Smoothed surface of two datasets

The smoothed surfaces of two point clouds are shown in Figure 6. It suggests that the smoothed surfaces are basically the base planes of objects, and it is beneficial to use the smoothed surface instead of skeleton.

Based on the stimulus value in Formula 6, we calculate SIDM value of each scale to measure its perceptual degradation. In Figure 7, there is a step change in SIDM values of multi-scales (e.g., between scale 4 and scale 5). This suggests that the stimulus variations caused by deleting small scale features (e.g., scale 2, 3, 4) are not enough be noticeable for human vision. This is in accord with the visual characteristics. The objective of the paper is to extract least points to describe the most perceptual information. Hence we select scale 4 of General and Base datasets as the optimal scales.

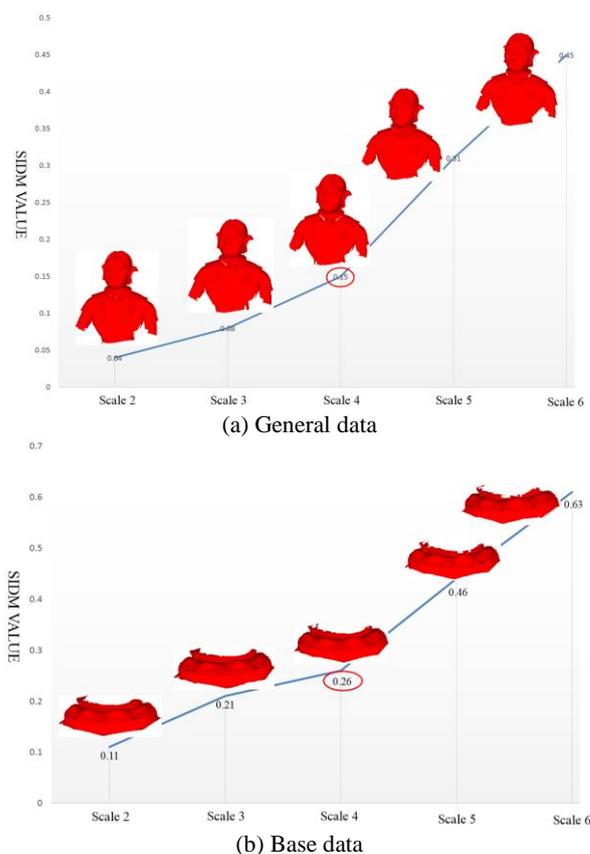


Figure 7. Optimal scale selection

5. CONCLUSIONS

Optimal information extraction of 3D point clouds is an inevitable process in various applications. This paper proposes

an effective method to extract optimal points from point cloud based on scale-adaptive reduction. The method introduces an importance metric by combining the surface variation and radial basis function. And then detect the edge outliers and extract points of multi-scale. Lastly, we propose a new stimulus variation measurement to evaluate degeneration of each scale for optimal selection, leading to a good perceptual quality.

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