SURFACE SNOW DENSITY OF EAST ANTARCTICA DERIVED FROM IN-SITU OBSERVATIONS

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ABSTRACT:
Models based on physical principles or semi-empirical parameterizations have used to compute the firn density, which is essential for the study of surface processes in the Antarctic ice sheet. However, parameterization of surface snow density is often challenged by the description of detailed local characterization. In this study we propose to generate a surface density map for East Antarctica from all the filed observations that are available. Considering that the observations are non-uniformly distributed around East Antarctica, obtained by different methods, and temporally inhomogeneous, field observations are used to establish an initial density map with a grid size of 30x30 km² in which the observations are averaged at a temporal scale of five years. We then construct an observation matrix with its columns as the map grids and rows as the temporal scale. If a site has an unknown density value for a period, we will set it to 0 in the matrix. In order to construct the main spatial and temporal information of surface snow density matrix we adopt Empirical Orthogonal Function (EOF) method to decompose the observation matrix and only take first several lower-order modes, because these modes already contain most information of the observation matrix. However, there are a lot of zeros in the matrix and we solve it by using matrix completion algorithm, and then we derive the time series of surface snow density at each observation site. Finally, we can obtain the surface snow density by multiplying the modes interpolated by kriging with the corresponding amplitude of the modes. Comparative analysis have done between our surface snow density map and model results. The above details will be introduced in the paper.

1. INTRODUCTION
Firn density of Antarctica can fluctuate spatially and temporally. The errors will be introduced by density value when converting volume change to mass change (Arthern et al., 2010). Furthermore, changes in grain size, structure, snow particles and properties occur during the process of snow densification which is of fundamental important in many aspects of glaciology, including the climatic signals contained in deep ice cores. (Sugiyama et al., 2012). Driven by these factors, near-surface snow density and the process of firn densification have been studied by observations derived from field measuring or by theoretical and numerical methods, such as numerous snow densification models (Sugiyama et al., 2012).

At present, mass balance estimates of the Antarctic Ice Sheet are mainly derived from Altimetry, Gravimetry and Input-Output (IOM) methods. High-precise estimate of elevation change can be achieved by satellite altimetry measurements, which makes altimetry method thought to be more precise than other two methods. However, the determination of the snow density introduces errors to the conversion from volume to mass change (Shepherd et al., 2012). Previous estimates of the ice-mass change from the measured elevation change have followed diverse criteria. Some authors adopted an effective density ranging from 350 to 917 kg/m³. Some apply firn correction models based physical principles or semi-empirical parameterizations (Gunter et al., 2009; Rignot et al, 2011; Shepherd et al., 2012; Zwally, 2015). So far, the biggest uncertainty from volume to mass change is density, according to Shepherd et al. (2012), the error introduced by selected density for the mass balance estimated by altimetry can be up to 30%. The firn density leads to more uncertainty for East Antarctica mass estimate.

The snow density profile is usually measured through following four methods. Traditional gravimetric method as the earliest way for Antarctic snow density measurement mainly aims to measure mass and volume (Hawley et al., 2008). According to the study, the resolution and accuracy depend on the sample size (Hawley et al., 2008). Comparing to the means by using a sampler (generally a rectangular sampler with a standard volume of 500 cm³) and a weight-balance, samples taken from ice cores can get deeper layer density values and obtained density generally is affected by the extracted core quality determined by diameter, length and weighted pieces of the core. During drilling, the mixing of snow layers will introduce errors, therefore, it is better to determine the snow density of the upper layer by using shallow pit measurements. In the neutron-scattering probe (NP) method, the density profiles are obtained by counting the rate of neutron returning to the detector and are largely affected by the diameter of the borehole (Hawley et al., 2008). Morris et al. (2008) pointed out that the 10% error of the borehole diameter in the derived density will be of the order 8-10%. In the dielectric profiling (DEP) method, density profiles are inferred by measuring conductivity and permittivity, and generally are subjected to core diameter effects (Hawley et al., 2008). Hawley and others (2008) indicated that errors occur in low-density sections can up to 15% and 10-13% for high-density sections. In the core optical stratigraphy (COS) method,

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density profiles are derived from extracting a similar core optical stratigraphy by use of digital photography to image core profiles and fine-scaled features are well captured by it (Hawley et al., 2008). NP, DEP and COS methods all provide tremendous improvements to traditional gravimetric method for density measurement with increased spatial resolution and accuracy. However, the application of these methods hasn’t yet spread and only a few observations exist. Due to the vertical density profiles are scarce over the entire Antarctica, we get the near-surface snow density map from all field observations that are available.

In this paper, we present a near-surface snow density map of East Antarctica from in-situ observations by using Empirical Orthogonal Function (EOF) to extract the most information of observations that contain time series of density.

2. DATA AND METHOD

2.1 Density Observations

2.1.1 Data Collection

We collected snow density data from all field observations that are available, including ice cores and snow pits. There are 2239 observations in total and span from 1957 to 2015 (Fig.1). This dataset contains 28 traverse routes and 1431 observation sites with only one density value at a time.

![Figure 1. Locations of 2239 in-situ observations used in the map of surface snow density](image)

2.1.2 Data Pre-processing

Near-surface densification has been studied by measuring the vertical profiles of firm cores and shallow pits (Sugiyama et al., 2012). These studies have found that the density changes with the depth and finally reaches the density of the ice. Considering that the depths of measured densities are different and the observations are non-uniformly distributed around Antarctica, following strategies had been taken to get neat data.

2.1.2.1 Unify the Depth of Density Values

We fit depth-density observations to get the average of observed density from 0-to2-meter depth for each density profile when needed. If the number of observations in a profile from 0-to3-meter depth is more than 5, we use a linear fit and then get the 0-to2-meter average density. If the number is smaller than 5 and there are observations from 0 to 1 meter or 2 meters, we will directly average the observations from 0-to2-meter depth. Otherwise, we average the density observations from 0-to1-meter depth or use the exponential function model in Takahashi et al. (2007) to fit the profile and average the observations from 0-to2-meter depth. However, initial layers’ depths of the two sites on the ITASE traverse route beyond 2 meters, they should have been rejected but due to the important spatial location, we accept them by fitting and then averaging the observations from 0-to3-meter depth.

2.1.2.2 Smooth the Observations

Next, removing the observations that beyond triple root mean square error for each traverse route and the density values were smoothed by a 30km running average to remove spatial and measurement noise for the traverse route that haven’t done before. But the 150km line measured by France locates on coastal area and has fast-changing densities, so we use segmented running average for it to retain the changeable high-density information. After that, all densities are averaged inside a 30 km x 30 km cell at each year and also averaged about every five years at each observation site.

2.1.2.3 Construct Observation Matrix

Last, we make up the observation matrix in which each column is one surface density map for a period, and each row is a time series of observations for a given site. If a site has an unknown density value for a period, we will set it to 0 in the matrix. The arrangement of the observation matrix is arranged in zigzag.

2.2 Method

2.2.1 Matrix Completion Algorithm

In order to analyse spatial and temporal variations of density, the observation matrix is needed to be completed, which can be regarded as a special case of matrix recovery problem. If a number of known entries are given, it is possible to recover the missing entries of matrix (Chen et al., 2010). The main solution strategy of this problem is based on the minimization of the nuclear norm, which requires singular value decomposition. In many applications, it is reasonable to assume that the matrix to be recovered is low-rank (Chen et al., 2010). In this paper, we make use of three methods to recovery observation matrix, they are LMaFit (Wen et al., 2012), IALM (Chen et al., 2010) and FPCA (Ma et al., 2011), respectively. Each method is run for several times to take out the result with the highest sampling rate and the minimum error of mean square. At the end, there may be very little data in the matrix that is not recovered, in this case we will use the average of density observations for a site to represent the missing density of a period. Prior to matrix completion, retain some known data for cross-validation to ensure the accuracy of matrix completion, and the result of cross-validation will be shown later.

2.2.2 Empirical Orthogonal Function

EOF is an effective method for analysing the spatial and temporal variations of the geophysical field (Björnsson et al., 1997). It identifies linear transformations of the geophysical field and concentrates as much variance as possible to a few variables (Preisendorfer et al., 1988) and has been widely used in oceanographic and meteorological analyses. After matrix completion, a full surface snow density matrix can be got with the time series of surface snow density at each observation site. In this study, we adopt EOF method to decompose the observation matrix and only take first several lower-order modes, because these modes already contain most information of the observation matrix. Finally, a map of surface snow
density covering about 97.9% of the East Antarctic area can be generated by multiplying the modes interpolated by kriging and the corresponding amplitude of the modes.

3. RESULT AND DISCUSSION

3.1 Results

3.1.1 Pre-processing Results
In order to ensure that densities come from same depth, we processed the data and get the mean densities from the surface to 2m depth. But there are still a few sites cannot obtain the average density value, we took the density at a particular depth within 0 to 2m. A total of 10 observations were removed and 2229 observations were remained as shown in Fig. 2.

3.1.2 Cross Validation Results
In the initial experiment, we separately produced the near-surface density maps of the East and West Antarctica since obtaining time for in-situ observations are quite different for them. For East Antarctica, we retained 7 observations, which are almost evenly distributed in space and time as shown in Fig. 3, for cross-validation to evaluate the accuracy of matrix completion.

The cross-validation result is the mean difference between density observation and recovered data is \(33.4\, \text{kg/m}^3\) with root mean square error about \(41.2\, \text{kg/m}^3\).

3.1.3 A Map of Surface Density
The preliminary result of East Antarctic near-surface snow density map is shown in Figure 4. It presents the average surface density from 1991 to 2015.

3.2 Comparative Analysis
We compared the difference between our East Antarctic density map and the modelled density map, that is calculated according to the method described by Ligtenberg et al. (2011) at the same time period. Modelled result is shown in Figure 5(a) and the differences between our result and model is shown in Figure 5(b). The difference, from \(122\, \text{kg/m}^3\) to \(-138\, \text{kg/m}^3\), between our result and the model is obviously. Big differences mainly locate in coastal area due to less observations but huge density variation around coast.

Figure 2. Locations and densities of 2229 observations after pre-processing

Figure 3. The density observations (black dots) at East Antarctica and green stars are the observation sites that can be used for cross-validation.

Figure 4. East Antarctic near-surface snow density map

Figure 5. Comparison of near-surface snow density: (a) modelled density map, (b) difference between our result and modelled density map.
Figure 5. (a) Average modelled surface density from 1991 to 2015. (b) Difference between our result and model.

4. SUMMARY AND CONCLUSIONS

This paper provides new ways for the study of Antarctic surface density. A near-surface density map of East Antarctica is completely generated from in-situ density observations. We believe that the density information carried by the reliable in-situ observations is more credible than empirical models and parameters. The result of density model is different from our result and big differences are concentrated on the coastal region. The largest difference is -138kg/m³. Since there are very little observations collected from the coast, signals with fast changes in the density of the coast have not been extracted. Our results within the East Antarctica coincided well with the modelled result, with differences between -20 and 50 accounting for 77.7% of all differences. Afterwards, we will decompose the complementary observation matrix spanning from 1957 to 2015 by EOF to obtain a near-surface density map of entire Antarctica. It should be noted that the above summery is based on the preliminary data processing and analysis results.

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6. REFERENCES


