AN EFFICIENT INITIALIZATION METHOD FOR K-MEANS CLUSTERING OF HYPERSPECTRAL DATA

A. Alizade Naeini a, A. Jamshidzadeh b, *, M. Saadatseresht a, S. Homayouni c

a Department of Geomatic Engineering, Faculty of Engineering, University of Tehran, Tehran, Iran - (a.alizadeh, msaadat)@ut.ac.ir
b Department of Geomatic Engineering, Faculty of Engineering, University of Bojnord, Bojnord, Iran - a.jamshidzadeh@ub.ac.ir
c Department of Geography, University of Ottawa, Ottawa, Canada - saeid.homayouni@uOttawa.ca

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ABSTRACT:

K-means is definitely the most frequently used partitional clustering algorithm in the remote sensing community. Unfortunately due to its gradient descent nature, this algorithm is highly sensitive to the initial placement of cluster centers. This problem deteriorates for the high-dimensional data such as hyperspectral remotely sensed imagery. To tackle this problem, in this paper, the spectral signatures of the endmembers in the image scene are extracted and used as the initial positions of the cluster centers. Afterwards, the spectral signatures of the endmembers are obtained using the Minimum Volume Enclosing Simplex (MVES) algorithm. Eventually, these spectral signatures are used to initialize the k-means clustering algorithm. The proposed method is implemented on a hyperspectral dataset acquired by ROSIS sensor with 103 spectral bands over the Pavia University campus, Italy. For comparative evaluation, two other commonly used initialization methods (i.e., Bradley & Fayyad (BF) and Random methods) are implemented and compared. The confusion matrix, overall accuracy and Kappa coefficient are employed to assess the methods’ performance. The evaluations demonstrate that the proposed solution outperforms the other initialization methods and can be applied for unsupervised classification of hyperspectral imagery for landcover mapping.

1. INTRODUCTION

Classification can be categorized into two main groups of supervised and unsupervised classification methods. Although supervised methods lead to the better results, unsupervised or clustering techniques have been attracted a lot of attentions because they don’t need any training data and procedure (Melgani and Pasolli, 2013).

Among different clustering algorithms, partitional methods are one of the best techniques for high-dimensional data, e.g., hyperspectral data. This is mainly because they have lower complexity (Celebi et al., 2013). The k-means algorithm is undoubtedly the most widely used partitional clustering algorithm (Jain, 2010). However, k-means has two significant disadvantages. First, it is sensitive to the outlier and noise. Second, it is highly sensitive to the selection of the initial clusters. Adverse effects of improper initialization include empty clusters, slower convergence, and a higher chance of getting stuck in bad local minima. Fortunately, these two drawbacks can be alleviated using an appropriate initialization method (Celebi et al., 2013). The problem of the initialization can be addressed by either deterministic (Celebi et al., 2013) or heuristic methods (Abraham et al., 2008). Although heuristic methods like particle swarm optimization (PSO) may lead to the best results, they are time-consuming and may have less stability in high-dimensional data. Accordingly, deterministic methods have priority if they lead to an acceptable result.

To address the initialization problem, different methods have been proposed especially for hyperspectral imagery. In (Sun et al., 2013), an artificial bee colony algorithm is used to find the appropriate position of cluster centers in hyperspectral data. In another similar work, (Namin et al., 2013) used the PSO clustering algorithm in Minimum noise fraction space. The comparison of their results with the K-means clustering method showed better performance for the PSO initialization in minimum noise fraction feature space. In (Celebi et al., 2013), the authors compared different initialization methods for k-means. Although, they have shown Bradley and Fayyad’s method is one of the best initialization methods, it was also demonstrated that the popular initialization methods often perform poorly and that there are in fact strong alternatives to these methods.

In this paper, a new initialization method for hyperspectral data clustering using k-means has been proposed. In this method, first, the number of endmembers is estimated by using the HFC (Harsanyi et al., 1993) technique. Then the spectral signature of endmembers (i.e., initial position of cluster centers) is obtained based on the MVES method.

The rest of the paper is organized as follows. Section 2 presents a summary of k-means, HFC and MVES algorithms. Section 3 introduces our proposed method. Section 4 describes the experimental setup and results. Lastly, section 5 gives our conclusion.

2. THEORETICAL BACKGROUND

2.1 K-Means Clustering

K-means clustering (MacQueen, 1967) is a method commonly used to automatically partition a dataset into K groups. It proceeds by selecting K initial cluster centers and then iteratively refining them as follows. 1) First, each point is assigned to its closest cluster center, 2) Each cluster center Cj is updated to be the mean of its constituent points (Wagstaff et al., 2001). From the mathematical perspective, given a data set \( X = \{x_1, x_2, \ldots, x_N\} \) in \( \mathbb{R}^D \), i.e., N points (vectors) each with D attributes (components), K-means algorithm divides \( X \) into K exhaustive and mutually exclusive clusters \( P = \{p_1, p_2, \ldots, p_K\} \).

* Corresponding author.
\[ U_{i+1}^j P_j = X, \quad p_j \cap p_i = \emptyset \quad \text{for} \ 1 \leq i \neq j \leq K. \] This algorithm generates clusters by optimizing a criterion function. The most intuitive and frequently used criterion function is the Sum of Squared Error (SSE) given by:

\[ \text{SSE} = \sum_{i=1}^{K} \sum_{x_j \in p_i} \| x_j - c_i \|^2_2 \]  

(1)

Where \( \| \cdot \|_2 \) denotes the Euclidean (\( L_2 \)) norm and \( c_i = \frac{1}{|p_i|} \sum_{x_j \in p_i} x_j \) is the centroid of cluster \( p_i \) whose cardinality is \(|p_i|\). The optimization of (1) is often referred to as the minimum SSE clustering (MSSC) problem (Celebi et al., 2013). Based on application, different similarity measures can be used instead of Euclidean distance (ED). In this study, Spectral similarity value (SSV) (Farifteh et al., 2007), as one of the most successful similarity measures in hyperspectral data (Homayouni and Roux, 2004), is used. SSV combines brightness and shape similarity. It is a combined measure of Pearson correlation (PC) and ED measures.

### 2.2 HFC Method

A Neyman–Pearson detection theory-based eigen-thresholding method, referred to as the HFC method, was developed to determine the number of endmembers, which called Virtual Dimensionality (VD), in AVIRIS data (Harsanyi et al., 1993). It first calculated the sample correlation matrix \( K_{slat} \) and sample covariance matrix \( R_{slat} \) and then found the difference between their corresponding eigenvalues, where \( L \) is the number of spectral band in the image. Let \( \{\lambda_1 \geq \lambda_2 \geq \ldots \geq \lambda_{VD} \} \) and \( \{\lambda_1' \geq \lambda_2' \geq \ldots \geq \lambda_L \} \) be two sets of eigenvalues generated by \( R_{slat} \) and \( K_{slat} \), called correlation eigenvalues and covariance eigenvalues, respectively. By assuming that signal sources are nonrandom unknown positive constants and noise is white with zero mean, we can expect that:

\[ \lambda_i' > \lambda_i, \quad \text{for} \ i = 1, \ldots, VD \]  

(2)

\[ \lambda_i = \lambda_i, \quad \text{for} \ i = VD + 1, \ldots, L \]  

(3)

More specifically, the eigenvalues in the ith spectral channel can be related by

\[ \lambda_i' > \lambda_i > \sigma_{n_i}^2, \quad \text{for} \ i = 1, \ldots, VD \]  

(4)

and

\[ \lambda_i = \lambda_i = \sigma_{n_i}^2, \quad \text{for} \ i = VD + 1, \ldots, L \]  

(5)

Where \( \sigma_{n_i}^2 \) is the noise variance in the ith spectral channel (Chien and Qian, 2004). In order to determine the VD, Harsanyi et al formulated the problem of determination of VD as a binary hypothesis problem as follows:

\[ H_0 : z_i = \lambda_i - \lambda_m = 0, \quad \text{versus} \quad H_i : z_i = \lambda_i - \lambda_m > 0, \quad \text{for} \ i = 1, 2, \ldots, L. \]  

(6)

Where, the null hypothesis \( H_0 \) represents the case that the correlation eigenvalue is equal to its corresponding covariance eigenvalue. The alternative hypothesis \( H_i \) is for the case that the correlation eigenvalue is greater than its corresponding covariance eigenvalue. In other words, when \( H_i \) is true (i.e., \( H_0 \) fails), it implies that there is an endmember contributing to the correlation eigenvalue in addition to noise, since the noise energy represented by the eigenvalue of \( R \) is in that particular component is the same as the one represented by the eigenvalue of \( K \) in its corresponding component.

Despite the fact that the \( \lambda_i \) and \( \lambda_i' \) are unknown constants, we can model each pair of eigenvalues \( \lambda_i \) and \( \lambda_i' \) under hypothesis \( H_0 \) and \( H_i \) as random variables by the asymptotic conditional probability densities given by

\[ p_{0}(z_i) = p(z_i | H_0) \equiv N(0, \sigma_{n_i}^2), \quad \text{for} \ i = 1, 2, \ldots, L \]  

(7)

and

\[ p_{i}(z_i) = p(z_i | H_i) \equiv N(\mu_i, \sigma_{n_i}^2), \quad \text{for} \ i = 1, 2, \ldots, L \]  

(8)

respectively, where \( \mu_i \) is an unknown constant and the variance \( \sigma_{n_i}^2 \) is given by

\[ \sigma_{n_i}^2 = \text{Var}[\lambda_i - \lambda_m] = \text{Var}[\lambda_i'] + \text{Var}[\lambda_m] - 2\text{Cov}(\lambda_i', \lambda_m) \]  

(9)

for \( i = 1, 2, \ldots, L \).

Eventually, they defined the false-alarm probability and detection power (i.e., detection probability) by using above mentioned equations and some approximations as follow:

\[ P_T = \int_{\tau_i}^{\infty} p_T(z) dz \]  

(10)

\[ P_D = \int_{\tau_i}^{\infty} p_T(z) dz \]  

(11)

A Neyman–Pearson detector for \( \lambda_i' - \lambda_m \), denoted by \( \delta\alpha_0(\lambda_i' - \lambda_m) \), in the binary composite hypothesis testing problem can be obtained by maximizing the detection power \( P_T \) in (11), while the false-alarm probability \( P_D \) in (10) is fixed at a specific given value, \( \alpha \), which determines the threshold value \( \tau_i \) in (10) and (11). So, a case of \( \lambda_i' - \lambda_m > \tau_i \), indicating that \( \delta\alpha_0(\lambda_i' - \lambda_m) \) fails the test, in which case there is signal energy assumed to contribute to the eigenvalue \( \lambda_i' \) in the ith data dimension. It should be noted that the test for hypothesis must be performed for each of \( L \) data dimensions. Therefore, for each pair of \( \lambda_i' - \lambda_m \), the threshold \( \tau \) is different and should be \( i \)-dependent, i.e., \( \tau_i \) (Chien and Qian, 2004).

### 2.3 MVES Algorithm

Minimum Volume Enclosing Simplex (MVES) is an unmixing algorithm without requiring the pure-pixel assumption, which estimates the endmembers by vertices of a minimum-volume simplex enclosing all the observed pixels. Linear mixture model is a widely used approach for spectral unmixing of remotely sensed hyperspectral imagery. Let \( M \) be an \( L \times P \) endmember signature matrix denoted by \( \{m_1, \ldots, m_p\} \), where \( m_i \) is an \( L \times 1 \) column vector represented by the signature of the ith material resident in the image scene, and \( P \) is the number of materials in the image scene. In linear mixture model, spectral signature of a pixel vector \( \mathbf{r} = (r_1, r_2, \ldots, r_L)^T \) can be represented by a linear regression model as follows:

\[ \mathbf{r} = \sum_{i=1}^{P} a_i \mathbf{m}_i + \mathbf{n} = \mathbf{M} \mathbf{a} + \mathbf{n} \]  

(12)

In the equation above, \( \mathbf{a} = (a_1, a_2, \ldots, a_P)^T \) is a \( P \times 1 \) column abundance vector associated with \( \mathbf{r} \), and \( \mathbf{n} = (n_1, n_2, \ldots, n_L)^T \) is a noise vector that can be interpreted as a measurement error (Heinz and Chein, 2001). The final goal of a spectral unmixing method is to recover the matrix \( \mathbf{M} \) and the endmember fractional abundance \( \mathbf{a} \) for each observed pixel. To do so, usually, noise needs to be minimized (in least squares fashion), and the volume of the...
simplex spanned by the columns of matrix $\mathbf{M}$ should be minimized (Winter, 1999). In MVES algorithm, Craig’s unmixing criterion (Craig, 1994) was employed to formulate the hyperspectral unmixing as an MVES optimization problem. 

The key property of this method is that all the dimension-reduced pixels $\mathbf{r}_i$ for $i = 1, \ldots, N$, must be inside the simplex constructed by the dimension-reduced endmembers $\alpha_i$ for $i = 1, \ldots, P$. This concept is illustrated in figure 1.

$$
\begin{align*}
\min_{\beta_1, \ldots, \beta_P} & \quad V(\beta_1, \ldots, \beta_P) \\
\text{s.t.} & \quad \mathbf{r}_i \in \text{conv}\{\beta_1, \ldots, \beta_P\}, \forall i
\end{align*}
$$

(13)

Where $V(\beta_1, \ldots, \beta_P)$ is the volume of the simplex $\text{conv}\{\beta_1, \ldots, \beta_P\} \subseteq \mathbb{R}^{P-1}$ given by

$$
V(\beta_1, \ldots, \beta_P) = \frac{|\det(\Delta(\beta_1, \ldots, \beta_P))|}{(P-1)!}
$$

(14)

Where

$$
\Delta(\beta_1, \ldots, \beta_P) = \begin{bmatrix} \beta_1 & \ldots & \beta_P \\ 1 & \ldots & 1 \end{bmatrix}
$$

(15)

Where $\Delta(\beta_1, \ldots, \beta_P)$ is always a square matrix, since the dimension-reduced pixels and endmembers are in a $p-1$ dimensional space. 

A cyclic minimization algorithm for approximating the MVES problem was developed using linear programs (LPs), which can be practically implemented by readily available LP solvers (Chan et al., 2009).

3. PROPOSED METHODS

In order to clustering of hyperspectral data, in this study, a multi-step framework was presented to resolve the problem of initialization of k-means and improve the clustering efficiency. The stages of this proposed method, namely, MVES initialization method has been illustrated in figure 2.

![Figure 1. Scatter plot of two-dimensional dimension-reduced pixels illustrating the MVES problem for hyperspectral unmixing (Chan et al., 2009)](image)

This figure also demonstrates that dimension-reduced pixels $\mathbf{r}_i$ can also be enclosed by a different simplex, denoted by $\text{conv}\{\beta_1, \ldots, \beta_P\}$. Nevertheless, by intuitive grounds, one would expect that the data enclosing simplex with the minimum volume should coincide with the true endmember simplex $\text{conv}\{\alpha_1, \ldots, \alpha_P\}$. This is exactly the belief of Craig’s unmixing criterion (Craig, 1994). The problem of finding the MVES can be formulated as an optimization problem as follows (Chan et al., 2009):

4. DISCUSSION AND RESULTS

4.1 Dataset

Experiments are performed using the ROSA University data set. This data set was acquired by the ROSIS sensor during a flight campaign in 2003 over the campus of Pavia University in the north of Italy. This data contains 610 by 340 pixels with 103 spectral bands. The geometric resolution is 1.3 m. nine ground-truth classes were considered in the experiments: Trees, Gravel, Meadows, Asphalt, Metal sheets, Bricks, Bitumen, Shadows and Bare soil. Figure 3 shows the ground-truth map and a color composite image of this data set.

![Figure 2. MVES Initialization method](image)

![Figure 3. ROSIS hyperspectral dataset over Pavia University used in experiments: (a) colour composition image (R: 60, G: 30, B: 10). (b) Ground truth map.](image)
random methods. In the first step of the new method, the number of endmembers is estimated by HFC algorithm as 9. The false alarm probability for this detection problem is set to 0.001. As it is said earlier, among different similarity measures for k-means clustering, SSV is used here in all three cases.

In the first case, initial position of cluster centers are obtained using Bradley & Fayyad (BF) method (Bradley and Fayyad, 1998). According to (Celebi et al., 2013), this method is one of the best methods for k-means initialization in different datasets, and as a result, it is used here to be compared with our proposed method. BF method starts by randomly partitioning of the dataset into J=10 subsets. Clustering results of this case are tabulated in table 1.

Table 1. Confusion matrix based on BF initialization method.

According to table 1, both Gravel and Asphalt classes have not been recognized. That’s why Gravel class has spectral signatures nearly the same as Bricks class on the one hand, and on the other both Asphalt and bitumen have nearly the same spectral signatures. Figure 4 and 5 show these spectral similarities.

In the second case, cluster centers are randomly initialized. Clustering results in this case have been shown in table 2.

Table 2. Confusion matrix based on Random initialization method.

Like the first case, both Gravel and Asphalt classes have not been discriminated in this case. This is because of the above-mentioned reasons.

In the third case, initial position of cluster centers are obtained using MVES method. Clustering results of this case have been shown in table 3.

Table 3. Confusion matrix based on MVES initialization method.

According to table 3, this case leads to highly better results than the other cases. As is obvious, using MVES method not only the best kappa coefficient are obtained but also Asphalt and Bitumen classes are discriminated. For comparative purpose, kappa coefficients and overall accuracies for three cases above are shown in figure 6.

As shown in figure 6, among these three methods, our proposed method with kappa coefficient of 55.3 leads into better result than BF and random methods with kappa coefficients of 3.09 and 31.5 respectively. Furthermore, unlike both BF and random method,
our proposed method is independent of iterations. In other words, our proposed method leads to the same result in different iterations.

5. CONCLUSION

In order to clustering of hyperspectral data, in this study, a multi-step framework was presented to resolve the problem of initialization of k-means and improve the clustering efficiency. In the first step, HFC is used to estimate the number of endmembers in the image. Then, the spectral signatures of the endmembers are obtained using the MVES algorithm. Lastly, these spectral signatures are used to initialize the k-means clustering algorithm. The proposed method has been compared with two well-known initialization methods, namely, BF and Random methods. Clustering using MVES initialization method with number and identity of spectral endmembers: An integrated approach using Neyman-Pearson eigen-thresholding and iterative constrained RMS error minimization.

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REFERENCES


